Lecture 6 Logic Gates and Circuits

Goals

- Identify the basic gates and describe the behavior of each gate
- Describe how gates are implemented using transistors
- Combine basic gates into circuits
- Describe the behavior of a gate or circuit using Boolean expressions, truth tables, and logic diagrams

Computers and Electricity

Gate

A device that performs a basic operation on electrical signals.

Circuits

Gates combined to perform more complicated tasks.

Computers and Electricity

How do we describe the behavior of gates and circuits?

Boolean expressions

Uses Boolean algebra, a mathematical notation for expressing two-valued logic

Logic diagrams

A graphical representation of a circuit; each gate has its own symbol

Truth tables

A table showing all possible input value and the associated output values

Gates

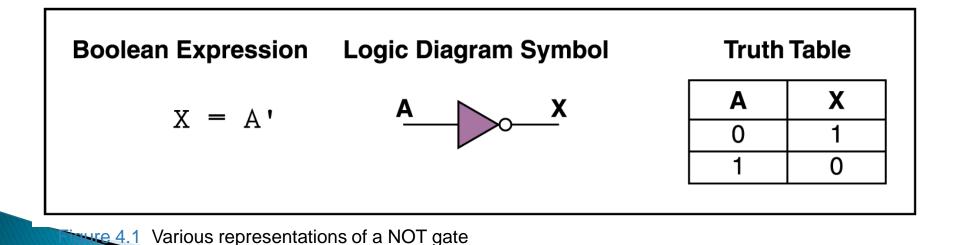
Six types of gates

- NOT
- AND
- OR
- XOR
- NAND
- NOR

Typically, logic diagrams are black and white with gates distinguished only by their shape We use color for emphasis (and fun)

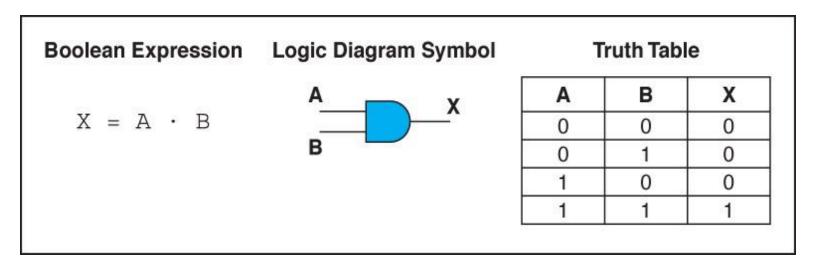
NOT Gate

A NOT gate accepts one input signal (0 or 1) and returns the opposite signal as output



AND Gate

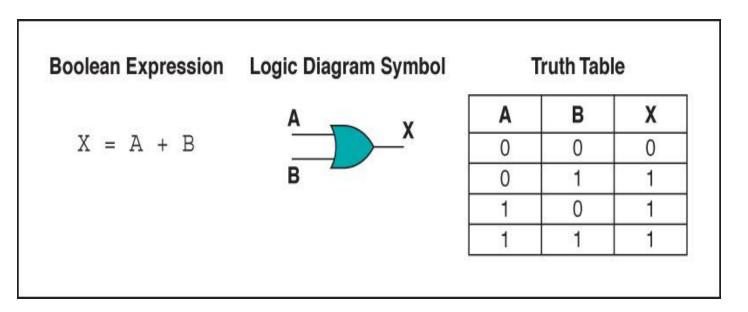
An AND gate accepts two input signals If both are 1, the output is 1; otherwise, the output is 0



Eigure 4.2 Various representations of an AND gate

OR Gate

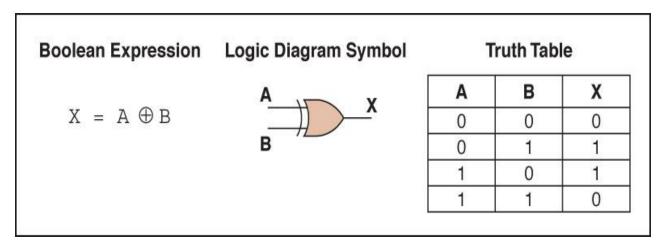
An OR gate accepts two input signals If both are 0, the output is 0; otherwise, the output is 1



Various representations of a OR gate

XOR Gate

An XOR gate accepts two input signals If both are the same, the output is 0; otherwise, the output is 1





XOR Gate

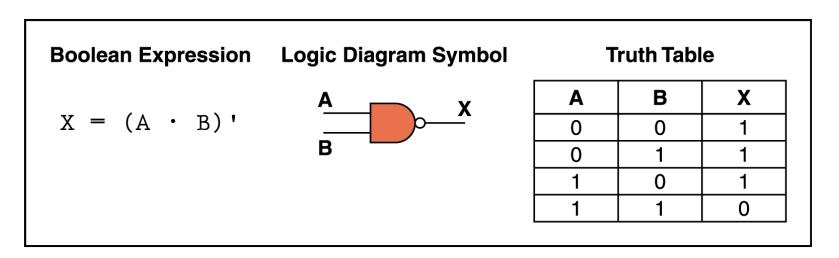
Note the difference between the XOR gate and the OR gate; they differ only in one input situation

When both input signals are 1, the OR gate produces a 1 and the XOR produces a 0

XOR is called the *exclusive OR*

NAND Gate

The NAND gate accepts two input signals If both are 1, the output is 0; otherwise, the output is 1



Eigure 4.5 Various representations of a NAND gate

NOR Gate

The NOR gate accepts two input signals If both are 0, the output is 1; otherwise, the output is 0

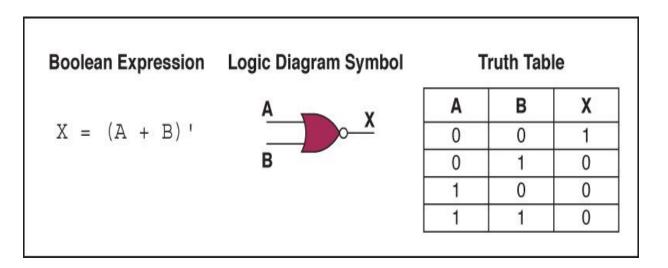


Figure 4.6 Various representations of a NOR gate

Review of Gate Processing

A NOT gate inverts its single input

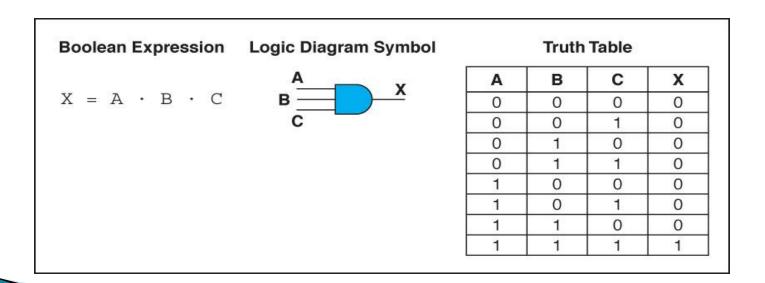
- An AND gate produces 1 if both input values are 1
- An OR gate produces 0 if both input values are 0
- An XOR gate produces 0 if input values are the same

A NAND gate produces 0 if both inputs are 1 A NOR gate produces a 1 if both inputs are 0

Gates with More Inputs

Gates can be designed to accept three or more input values

A three-input AND gate, for example, produces an output of 1 only if all input values are 1



Constructing Gates

Transistor

- A device that acts either as a wire that conducts electricity or as a resistor that blocks the flow of electricity, depending on the voltage level of an input signal
- A transistor has no moving parts, yet acts like a switch
- It is made of a semiconductor material, which is neither a particularly good conductor of electricity nor a particularly good insulator

Constructing Gates

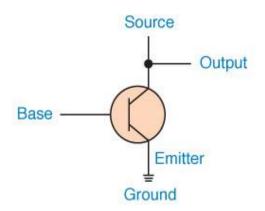
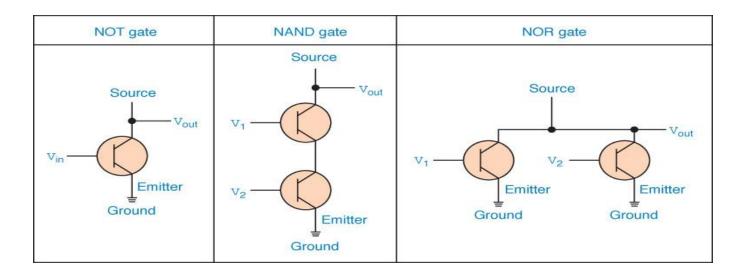


Figure 4.8 The connections of a transistor

A transistor has three terminals A source A base An emitter, typically connected to a ground wire If the electrical signal is grounded, it is allowed to flow through an alternative route to the ground (literally) where it can do no harm

Constructing Gates

The easiest gates to create are the NOT, NAND, and NOR gates



Circuits

Combinational circuit

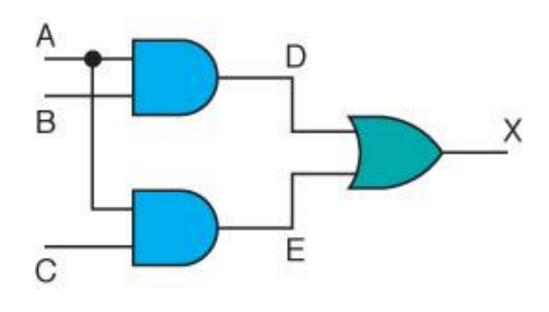
The input values explicitly determine the output

Sequential circuit

- The output is a function of the input values and the existing state of the circuit We describe the circuit operations using
- Boolean expressions Logic diagrams
 - Truth tables

Are you surprised?

Gates are combined into circuits by using the output of one gate as the input for another



Α	в	С	D	Е	X
0	0	0	0	0	0
0	0	1	0	0	0
0	1	0	0	0	0
0	1	1	0	0	0
1	0	0	0	0	0
1	0	1	0	1	1
1	1	0	1	0	1
1	1	1	1	1	1

Three inputs require eight rows to describe all possible input combinations This same circuit using a Boolean expression is (AB + AC)

Consider the following Boolean expression A(B + C)

	Α	в	С	B + C	A(B + C)
A(D+0)	0	0	0	0	0
	0	0	1	1	0
	0	1	0	1	0
	0	1	1	1	0
	1	0	0	0	0
D+0	1	0	1	1	1
	1	1	0	1	1
	1	1	1	1	1

Does this truth table look familiar?

Compare it with previous table

Circuit equivalence

- Two circuits that produce the same output for identical input
- Boolean algebra allows us to apply provable mathematical principles to help design circuits
- A(B + C) = AB + BC (distributive law) so circuits must be equivalent

Properties of Boolean Algebra

Property	AND	OR
Commutative	AB = BA	A + B = B + A
Associative	(AB)C = A(BC)	(A + B) + C = A + (B + C)
Distributive	A(B + C) = (AB) + (AC)	A + (BC) = (A + B) (A + C)
Identity	A1 = A	A + 0 = A
Complement	A(A') = 0	A + (A') = 1
DeMorgan's law	(AB) ' = A' OR B'	(A + B)' = A'B'

Integrated Circuits

Integrated circuits (IC) are classified by the number of gates contained in them

Abbreviation	Name	Number of Gates
SSI	Small-Scale Integration	1 to 10
MSI	Medium-Scale Integration	10 to 100
LSI	Large-Scale Integration	100 to 100,000
VLSI	Very-Large-Scale Integration	more than 100,000

Integrated Circuits

Integrated circuit (also called a *chip*)

A piece of silicon on which multiple gates have been embedded

Silicon pieces are mounted on a plastic or ceramic package with pins along the edges that can be soldered onto circuit boards or inserted into appropriate sockets

Integrated Circuits

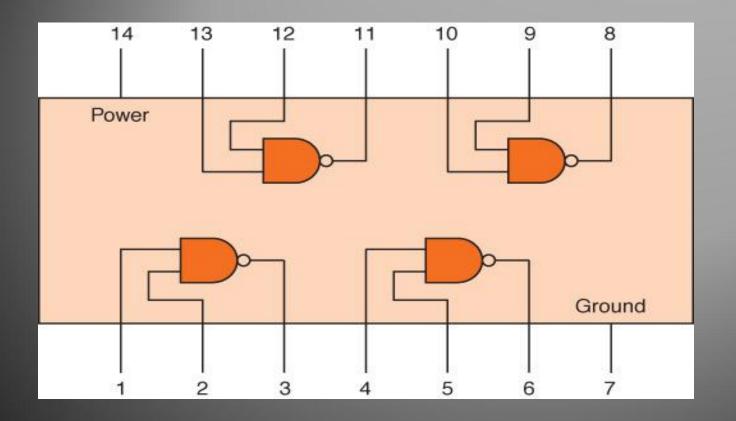


Figure 4.13 An SSI chip contains independent NAND gates

CPU Chips

The most important integrated circuit in any computer is the Central Processing Unit, or CPU
Each CPU chip has a large number of pins through which essentially all communication in a computer system occurs

Logic Gates

